Ideas from Kit Fine’s theory of arbitrary objects are applied to questions concerning mathematical structuralism. I discuss how sui generis mathematical structures can be viewed as generic systems of mathematical objects, where mathematical objects are interpreted as arbitrary objects in Fine’s sense. For definiteness, I will concentrate in this context on the generic omega-sequence as the subject matter of arithmetic.